University of North Georgia Sophomore Level Mathematics Tournament April 11, 2015

You have 200 cookies. You give them to your friends in such a way that each friend gets at least one cookie and no two friends get the same number of cookies.

What is the largest number of friends that can receive cookies?

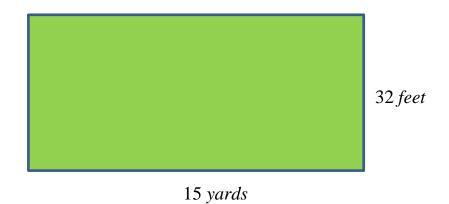


If you need this document in another format, please email <u>minsu.kim@ung.edu</u> or call 678-717-3546.

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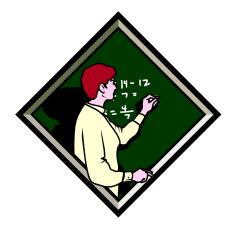
This lawn's area will be increased 15% in size. How many extra square *yards* will be added?

•



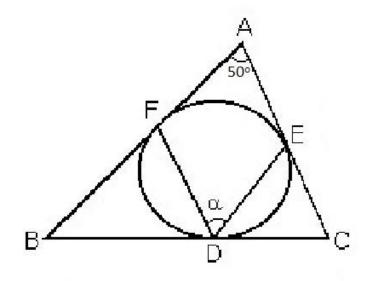
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Consider a sample of 10 marbles drawn from a bin that has red and green marbles. The probability that any marble we draw is red is  $\mu = 0.55$  (independently, with replacement). We draw 656 independent samples. What is the probability that at least one of the samples has all green marbles? Give your answer to the nearest thousandth.



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In the figure below, *ABC* is a triangle with a circle inscribed and  $\angle BAC = 50^{\circ}$ .  $\overline{AB}$  is tangent to the circle at point *F*,  $\overline{AC}$  is tangent to the circle at point *E*, and  $\overline{BC}$  is tangent to the circle at point *D*, What is the angle  $\alpha$  ?

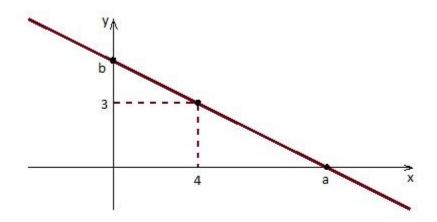


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Find the acute angle  $\Phi$  formed by the two lines y-3x = 0 and 2x-3y = 1. Give your answer to the nearest whole *degree*.

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Find (a-4)(b-3).

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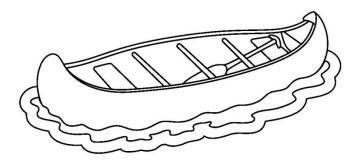
In a triangle *PQR*,  $\angle R = \frac{\pi}{2}$ . If  $\tan\left(\frac{P}{2}\right)$  and  $\tan\left(\frac{Q}{2}\right)$  are the roots of the equation

 $ax^2 + bx + c = 0$ ,  $a \neq 0$ , then find a relation between *a*, *b*, and *c*.



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Jane is in a canoe and is paddling upstream. After traveling 1 mile from her starting point, a log in the stream passes by her. She continues upstream for an additional hour and turns around. She arrives at her starting point at the same time as the log. How fast is the stream?



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Simplify 
$$A = \frac{\frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{99} + \frac{1}{100}}{\frac{1}{99} + \frac{2}{98} + \dots + \frac{99}{1}}$$
.

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*ABCDE* is a five distinct-digit even number that is less than 25,000. Given that none of the digits are 3 or 6, and that four times *ABCDE* is *EDCBA*, another even number, find *ABCDE*.

